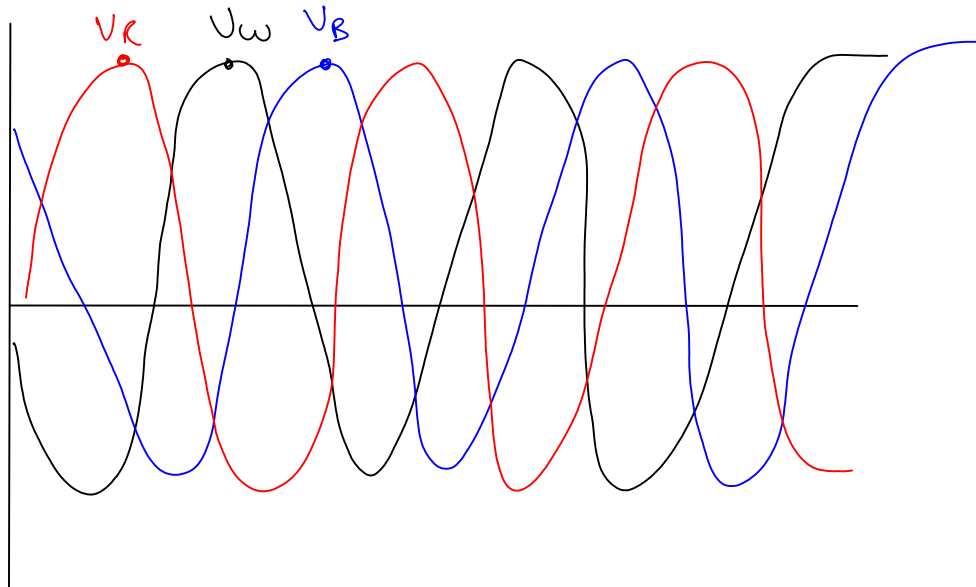
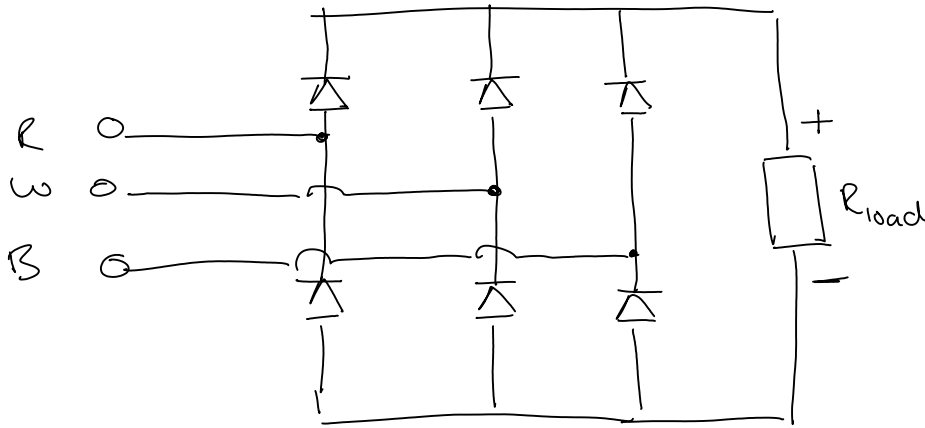


# Lecture 18

Tuesday, 13 October 2009  
4:53 PM

## 3 $\phi$ Full-wave Rectifier



$$V_r = V_m \sin \omega t$$

$$V_w = V_m \sin \left( \omega t - \frac{2\pi}{3} \right)$$

$$V_b = V_m \sin \left( \omega t - \frac{4\pi}{3} \right)$$

$$\text{For } \frac{\pi}{6} \leq \omega t \leq \frac{\pi}{2}$$

$$V_L = V_r - V_w = \sqrt{3} V_m \sin\left(\omega t + \frac{\pi}{6}\right)$$

$$V_{AVE} = \frac{1}{\frac{\pi}{2} - \frac{\pi}{6}} \int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \sqrt{3} V_m \sin\left(\omega t + \frac{\pi}{6}\right)$$

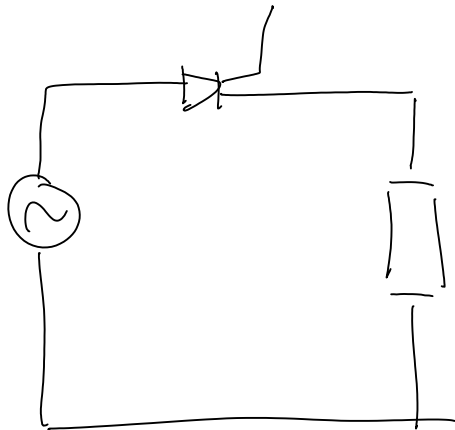
$$= \frac{6}{2\pi} \sqrt{3} V_m \left[ -\cos\omega t + \frac{\pi}{6} \right]_{\frac{\pi}{6}}^{\frac{\pi}{2}}$$

$$= \frac{3\sqrt{3} V_m}{\pi} \left[ -\left( \cos \frac{4\pi}{6} - \cos \frac{2\pi}{6} \right) \right]$$

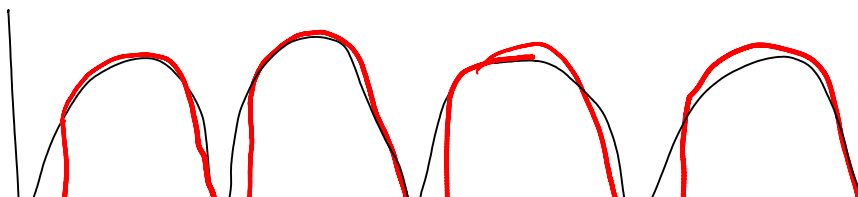
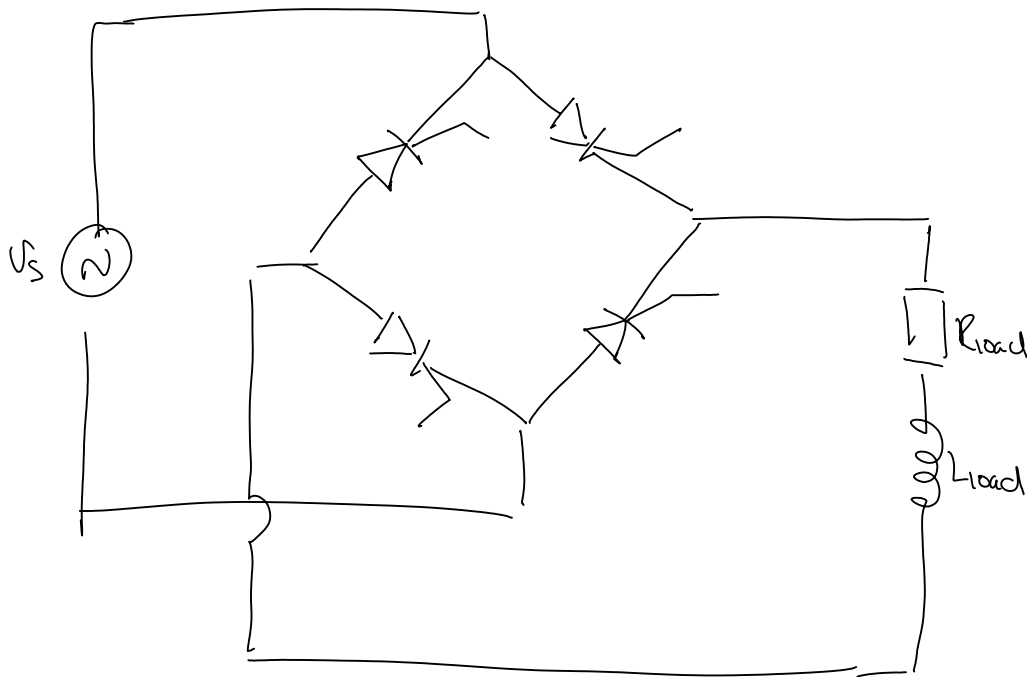
$$= \frac{3\sqrt{3} V_m}{\pi} \left[ -\left( -2 \cos \frac{\pi}{3} \right) \right]$$

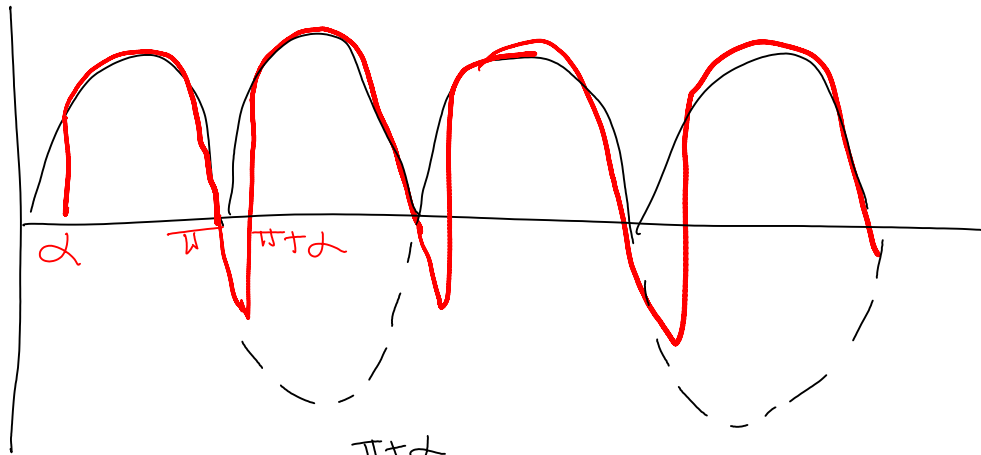
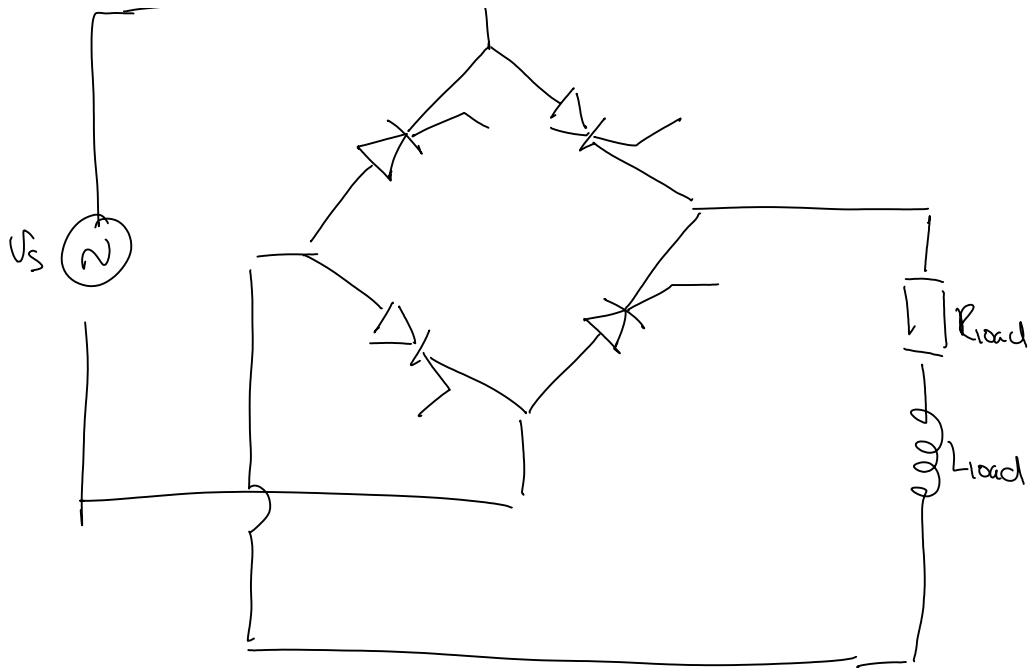
$$= \frac{3\sqrt{3} V_m}{\pi}$$

$\frac{1}{2}$  wave  $1\phi$  controlled rectifier



$$\begin{aligned}
 V_{AVE} &= V_{DC} \\
 &= \frac{1}{2\pi} \int_{\alpha}^{\pi} V_m \sin \omega t \, d(\omega t) \\
 &= \frac{V_m}{2\pi} \left[ -\cos \omega t \right]_{\alpha}^{\pi} \\
 &= \frac{V_m}{2\pi} - \left[ -1 - \cos \alpha \right] \\
 &= \frac{V_m}{2\pi} \left[ 1 + \cos \alpha \right] \\
 &= \frac{\sqrt{2} V_{rms}}{2\pi} (1 + \cos \alpha)
 \end{aligned}$$





$$\begin{aligned}
 U_{AVE} &= \frac{1}{\pi} \int_{\alpha}^{\pi+\alpha} U_m \sin \omega t \, d(\omega t) \\
 &= \frac{U_m}{\pi} \left[ -\cos \omega t \right]_{\alpha}^{\pi+\alpha} \\
 &= \frac{U_m}{\pi} \left[ -(\cos(\pi+\alpha) - \cos \alpha) \right] \\
 &= \frac{U_m}{\pi} \left[ -(-2 \cos \alpha) \right] \\
 &= 2U_m
 \end{aligned}$$

$$V_{AVE} = \frac{2V_m}{\pi} \cos \alpha$$

## EXAM STRUCTURE

1. T/F	36m
2. IM	36m
3. DC m/c	36m
4. PE	36m
5. Sensors	36m